

# Augmentation of thermohydraulic performance in a dimpled tube using ternary hybrid nanofluid

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**Abstract:** This computational study explores the thermal and hydraulic efficiency of heat exchanger tube configurations utilizing hybrid nanofluids and circular dimples. Seven distinct configurations incorporating different volumetric concentrations of three nanoparticles (GnP, MWCNT, and Fe<sub>3</sub>O<sub>4</sub>) and two circular dimple pitch ratios are examined. The investigation concentrates on crucial parameters, including Nusselt number, friction factor, and thermohydraulic performance. The numerical analysis specifically addresses single-phase flow within the Reynolds number range of 5000-30000, maintaining a constant surface heat flux during simulations. Notably, Nusselt number consistently rises with Reynolds number across all configurations. Friction factor analysis indicates minimal sensitivity to hybrid nanofluid ratios but an increase with circular dimples. Despite the elevated pressure drop, the thermohydraulic coefficient consistently surpasses 1, signifying a net energy gain from enhanced heat transfer. Optimal performance is observed in the S5- $P/Dt=1$  configuration, exhibiting the highest thermohydraulic coefficient at 1.35, while the  $P/Dt=2$  variation within the same fluid model presents a slightly lower value of 1.32.

**Keywords:** Hybrid nanofluid, heat transfer enhancement, circular dimple, thermohydraulic performance.

## 1. Introduction

Improving the efficiency of cooling and heating systems can be achieved by enhancing heat transfer. Research on the enhancement of heat transfer is essential to reduce energy losses in the increasing energy demand in the current century [1-2].

In general, inserts are placed in the flow passage to enhance the heat transfer rate, resulting in a reduction in the hydraulic diameter of the flow passage [3]. Heat transfer enhancement consists of two different techniques, active and passive. Heat transfer enhancement in active methods requires external inputs such as electrostatic fields, mechanical vibration, or pulsation [4]. Passive methods deal with surface shape modifications or intensify the flow turbulence to enhance the heat transfer [5,6]. Porous materials [7-9], corrugated surfaces [10-13], extended surfaces [14-16], dimples [17-21], inserts such as wire coils, swirl flow tools, protrusions [22-25], and nanofluids [26-28] are some examples of passive techniques.

Considering the thermal-hydraulic performance, it becomes clear how significant the passive method is. In industries, improving thermal contact and reducing pumping power are crucial in terms of efficiency and economy to design better heat exchangers. The studies in the literature about passive methods show significant results

in thermal-hydraulic performance. Vicente et al. [29,30] presented that roughness has a powerful impact on the enhancement of thermal performance and, energy efficiency in their two studies with dimpled tubes and corrugated tubes, respectively. Zheng et al. [31] represented that the appliance of the inclined grooved tube enhances the heat transfer and friction factor ( $f$ ) in the range of approximately 1.23 - 2.17 and 1.02 - 3.75 compared to smooth tubes, respectively. Chen et al. [32] analyzed the comparison of six different oriented dimpled copper tubes with a smooth tube. In their study, they tried to find the best performance according to the geometrical configuration of dimples. The maximum performance improvement has been found in the largest value of the ratio of the depth of the dimple to the inner diameter, the pitch of the dimple, and the number of dimples longitudinally. The heat transfer coefficient has improved between 1.25 - 2.37 times at a constant  $Re$ . In addition, the increase in  $f$  is between 1.08 to 2.35 higher than the smooth tube. In their study, the exponential Reynolds number ( $Re$ ) is between 0.883 and 0.934. Piper et al. [33] probed the dimpled surface to enhance the pillow-plate heat exchanger. They showed that a dimpled surface decreased the pressure drop by around 9%. Similarly, comparing the dimpled surface with a smooth surface, the mean heat transfer coefficient has improved by 2.2%, and thermo-hydraulic performance enhanced by 11.2%. Bi

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et al. [34] used two different heat passive methods dimples, grooves, and fins to improve heat transfer in their studies. In their study, apart from these three methods, they also examined different geometric configurations to select the most effective dimple. They showed that at lower  $Re$  of  $Re < 3323$  grooves have the highest value of PEC of around 1.35. However, dimple surfaces will reach the best performance of heat transfer augmentation as the  $Re$  increases. Moreover, the geometrical configuration of dimples in the study shows that the heat transfer enhancement is easier when the dimples are deeper with a large diameter. Xie et al. [21] analyzed the effect of cross ellipsoidal dimples on heat transfer based on different structural parameters. They indicated that although Nusselt number ( $Nu$ ) and  $f$  increase with the increase in the depth of the dimples, Performance Evaluation Criteria (PEC) decreases. Moreover, another parameter in the study shows that  $Nu$  is inversely proportional to pitch. Similarly, the largest PEC is obtained in the smallest pitch in this case. Similar to pitch, PEC is inversely proportional to the axis ratio. As a result of their study, they obtained the highest PEC as 1.58 at a constant  $Re$  of 5000 with the combination of three structural parameters. Corrugated surfaces, fins, and dimples provide heat transfer improvement up to some limits due to their low heat transfer performance. Using nanoparticles with these methods improves heat transfer augmentation. Kabeel et al. [35] examined the effect of nanoparticles on the corrugated surface in their study. They have used  $Al_2O_3$  nanomaterial in the water-based fluid with different volumetric concentrations (1-4%). In the study, the heat transfer coefficient increased up to 13% after adding nanomaterial with a 4% concentration. Khairul et al. [36] showed that using nanofluid of CuO with the corrugated surface enhanced the heat transfer coefficient up to 24.7%. Firoozi et al. [26] numerically investigated the heat transfer characteristics of nanofluid in 27 configurations of the dimple. They achieved the highest PEC of 2.50 and 3.12 for water and the flow of  $Al_2O_3$  nanofluid, respectively. Suresh et al. [37] experimentally showed that CuO/Water nanofluid enhanced the heat transfer coefficient 1.06 times and 1.15 times based on the concentration of the nanoparticles of 0.1% and 0.3% in the helically dimpled tube, respectively.

Recently, hybrid nanofluids are attracting more attention as a new heat transfer enhancement method. Hybrid nanofluid consists of two or more different nanoparticles. In the literature, it has been seen that hybrid nano-

fluids are more effective in improving heat transfer than monotype nanofluids [38]. There are several studies about hybrid nanofluids. Toghraie et al. [39] researched the effect of hybrid nanofluids on thermal conductivity. The study showed that ZnO-TiO<sub>2</sub> hybrid nanofluids in ethylene glycol enhanced the thermal conductivity by around 32%. Sundar et al. [40] experimentally observed that nanodiamond-nickel hybrid nanofluid in water base fluid enhanced the thermal conductivity and viscosity by around 29% and 23%, respectively compared to water. Moreover, the  $Nu$  enhancement is about 25% and 35% according to 0.1% and 0.3% volumetric concentration of hybrid nanofluid. Khan et al. [41] demonstrated that alumina/silica hybrid nanofluid achieved the maximum value of PEC as 1.24 in the mini channel heat sink. Ahmed et al. [42] numerically investigated the thermo-hydraulic performance of nanofluids in a dimpled channel. The result shows that the heat transfer coefficient is 35% for the dimpled channel and around 46%, 44%, and 42% for  $Al_2O_3$ ,  $Al_2O_3$ -CuO, and CuO nanofluids, respectively.

As it can be seen that different configurations of dimples and different passive methods are used in the literature review. In addition, heat transfer enhancement was made by using these passive methods with the combination of different nanofluids. As seen in these studies, it is possible to improve heat transfer at certain rates with different configurations of different methods. In this study, seven different configurations of hybrid nanofluids are studied from different volumetric concentrations of three (GnP, MWCNT, Fe<sub>3</sub>O<sub>4</sub>) nanoparticles. The most effective configuration is tried to be obtained by analyzing these seven different hybrid nanofluids in a pipe with a dimpled surface. In addition, graphene, carbon nanotube, and iron oxide nanoparticles with different geometrical shapes are studied as nanoparticles. The addition of iron oxide to these hybrid nanofluids will also allow for thermal performance modification using active methods in the future.

## 2. Materials and Method

### 2.1. Numerical model

The objective of this research is to investigate the thermo-hydraulic performance of a dimpled tube using CFD software, considering different ternary nanofluid compositions. The solution domain for a dimpled tube is illustrated in Figure 1, while Table 1 outlines the physical parameters of the numerical model.

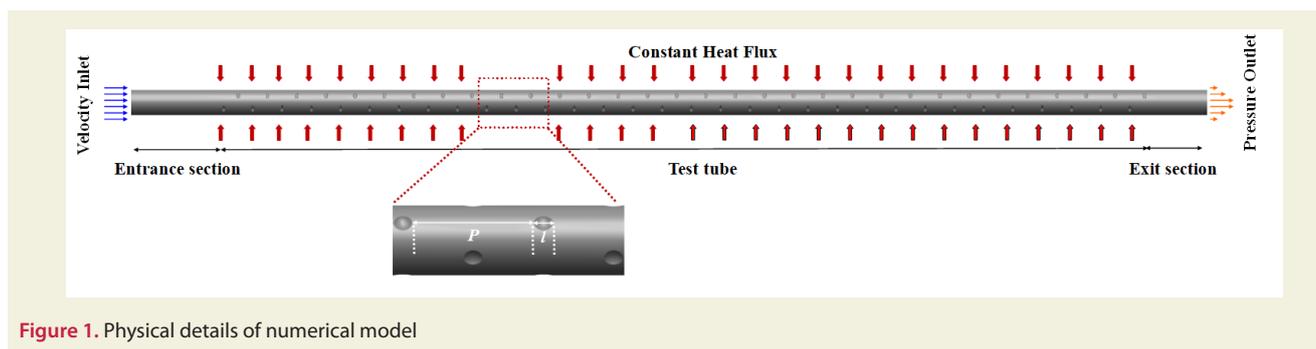


Figure 1. Physical details of numerical model

The numerical model consists of three sections: the inlet, the test, and the outlet. The inlet section generates flow hydrodynamically and prevents any disturbances at the entrance of the tube. The lengths of the inlet, test, and outlet sections are chosen to be 100 mm, 1000 mm, and 50 mm, respectively. The outer surface of the tube wall is exposed to a continuous heat flow of 20 kW/m<sup>2</sup>. The investigation involves the use of ternary hybrid nanofluid configurations flowing through the tube with *Re* ranging from 5000 to 30000. The numerical analyses consider parameters such as the pitch ratio ( $P/D_t = 1$  and 2) and nanoparticle loading fraction.

**Table 1.** Geometrical parameters of dimpled tube.

Geometric parameter	Value(mm)
Diameter of tube( $D_t$ )	15
Length of entrance section( $L_{ent}$ )	100
Length of test tube( $L_t$ )	1000
Length of exit section( $L_{ex}$ )	50
Length of dimple( $l$ )	4
Height of dimple( $h_d$ )	1.5
Pitch ratio ( $P/D_t$ )	1 and 2

## 2.2. Nanofluid configurations and thermophysical properties

In this study, the overall hybrid nanofluid volume ratio was set at 1.5%. The volumetric contribution levels of GnP, MWCNT, and  $FE_3O_4$  nanoparticles, which compose the hybrid nanofluid, were varied within the range of 0.25-0.75% to establish seven distinct fluid configurations as given in Table 2.

**Table 2.** The volumetric contribution levels of nanoparticles

No	Volume fractions			
	GnP	MWCNT	$FE_3O_4$	Total
S1	0.0050	0.0050	0.0050	0.015
S2	0.0050	0.0075	0.0025	0.015
S3	0.0050	0.0025	0.0075	0.015
S4	0.0025	0.0050	0.0075	0.015
S5	0.0075	0.0050	0.0025	0.015
S6	0.0025	0.0075	0.0050	0.015
S7	0.0075	0.0025	0.0050	0.015

**Table 3.** Thermophysical properties of ternary hybrid nanofluid components[43]

Properties	Water	GnP	MWCNT	$FE_3O_4$
$\rho$ (kg/m <sup>3</sup> )	998.2	2250	2100	5180
$C_p$ (J/kg K)	4182	790	710	104
$k$ (W/mK)	0.6	3000	2000	17.65

$$\mu_{Thnf} = \frac{\mu_f}{(1-\phi_1)^{2.5}(1-\phi_2)^{2.5}(1-\phi_3)^{2.5}} \quad (1)$$

$$\rho_{Thnf} = [(1-\phi_1)\{(1-\phi_2)[(1-\phi_3)\rho_f + \rho_3\phi_3] + \rho_2\phi_2\} + \rho_1\phi_1] \quad (2)$$

$$(\rho C_p)_{Thnf} = (1-\phi_1)\{(1-\phi_2)[(1-\phi_3)(\rho C_p)_f + (\rho C_p)_{s_3}\phi_3] + (\rho C_p)_{s_2}\phi_2\} + (\rho C_p)_{s_1}\phi_1 \quad (3)$$

$$\frac{k_{Thnf}}{k_{hnf}} = \frac{k_1 + 2k_{nf} - 2\phi_1(k_{nf} - k_1)}{k_1 + 2k_{nf} + \phi_1(k_{nf} - k_1)} \quad (4.a)$$

$$\frac{k_{hnf}}{k_f} = \frac{k_2 + 2k_{nf} - 2\phi_2(k_{nf} - k_2)}{k_2 + 2k_{nf} + \phi_2(k_{nf} - k_2)} \quad (4.b)$$

$$\frac{k_{nf}}{k_f} = \frac{k_3 + 2k_{nf} - 2\phi_3(k_{nf} - k_3)}{k_3 + 2k_{nf} + \phi_3(k_{nf} - k_3)} \quad (4.c)$$

The unique thermophysical characteristics of three distinct nanoparticles and the base fluid (water), as outlined in Table 3, were utilized to calculate the viscosity, density, specific heat, and thermal conductivity of the ternary hybrid nanofluid using the Equations 1-4, respectively. Subsequently, the thermophysical properties of the seven different configurations were determined and subjected to further analysis.

## 2.3. Solution methodology

In this research, numerical analysis was conducted using the finite volume method in ANSYS Fluent 18. The turbulence model employed was the  $k - \epsilon$  RNG (Re-Normalization Group), and the SIMPLE algorithm scheme was utilized to assess the correlation between pressure and velocity. For convection evaluation, the QUICK scheme was implemented. Convergence criteria for continuity, velocity, energy,  $k$ , and  $\epsilon$  values were set at  $1 \times 10^{-5}$ . The  $k - \epsilon$  RNG model, known for its precision among turbulence models, is based on three conservation equations of mass, momentum and energy, outlined in Equations 5, 6, and 7, respectively [44].

$$\nabla(\rho \vec{V}) = 0 \quad (5)$$

$$\nabla(\rho \vec{V} \vec{V}) = -\nabla P + \nabla(\mu \nabla \vec{V}) \quad (6)$$

$$\nabla(\rho c_p \vec{V} T) = \nabla(k \nabla T) \quad (7)$$

For the solution method RNG, the transport equations for  $k$  and  $\epsilon$  are given in Equations 8 and 9, respectively.

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left( \alpha_k \mu_{eff} \frac{\partial k}{\partial x_j} \right) + G_k + G_b - \rho \epsilon - Y_m + S_k \quad (8)$$

$$\frac{\partial}{\partial t}(\rho \epsilon) + \frac{\partial}{\partial x_i}(\rho \epsilon u_i) = \frac{\partial}{\partial x_j} \left( \alpha_\epsilon \mu_{eff} \frac{\partial \epsilon}{\partial x_j} \right) + C_{1\epsilon} \frac{\epsilon}{k} (G_k + C_{3\epsilon} G_b) - C_{2\epsilon} \rho \frac{\epsilon^2}{k} - R_\epsilon + S_\epsilon \quad (9)$$

Within these equations,  $G_k$  represents the production value of turbulent kinetic energy resulting from the velocity gradient, and  $G_b$  signifies the production value of turbulent kinetic energy arising from buoyancy. The parameters  $\alpha_k$  and  $\alpha_\varepsilon$  are defined as inverse effective Prandtl numbers for  $k$  and  $\varepsilon$ , respectively. Additionally,  $S_k$  and  $S_\varepsilon$  are characterized as user-input source data.

#### 2.4. Data reduction

In addition to computing the thermophysical properties of the hybrid nanofluids, these properties were defined and analyzed using the ANSYS Fluent 18 program. The obtained data from the analysis were used to calculate the  $Re$ ,  $Nu$ ,  $f$ , and thermohydraulic performance coefficient based on the following equations. Specifically, the  $Re$  was determined using Equation 10.

$$Re = \frac{\rho DV}{\mu} \quad (10)$$

The convective heat transfer coefficient is determined using Equation 11, where  $q'$  represents the applied heat flux over the flow field, and  $\Delta T$  denotes the temperature difference between the surface temperature of the flow field and the average temperature as the median of the inlet and the outlet fluid temperatures in the test tube.

$$h = \frac{q'}{\Delta T} \quad (11)$$

Following the computation of the heat convection coefficient, the  $Nu$  was determined using Equation 12.

$$Nu = \frac{hD}{k} \quad (12)$$

Yet another dimensionless parameter, the coefficient of friction, was computed using Equation 13.

$$f = \frac{\Delta P}{\frac{1}{2}\rho V^2 \frac{L}{D}} \quad (13)$$

The coefficient of thermohydraulic performance was calculated using Equation 14.

$$\eta = (Nu_{hnf}/Nu_b)(f_b/f_{hnf})^{1/3} \quad (14)$$

### 3. Results and Discussion

#### 3.1. Grid independence and validation of numerical methodology

To ensure the numerical results are independent of the number of cells, a grid independence study was conducted prior to the numerical analysis in this study. The impact of varying the number of cells on  $Nu$  and friction number at a  $Re$  of 5000 was investigated. The findings indicate that the deviation in  $Nu$  and  $f$  remained below 1% when the number of cells reached around 4.12 mil-

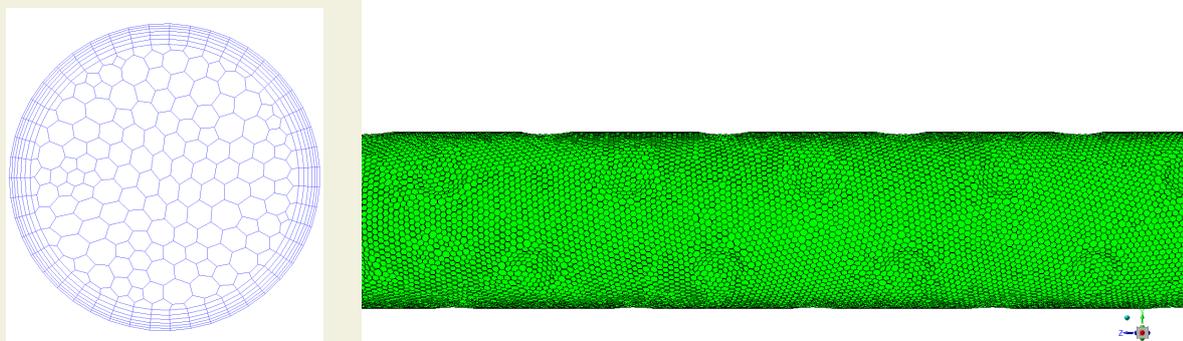


Figure 2. Grid structure of numerical model

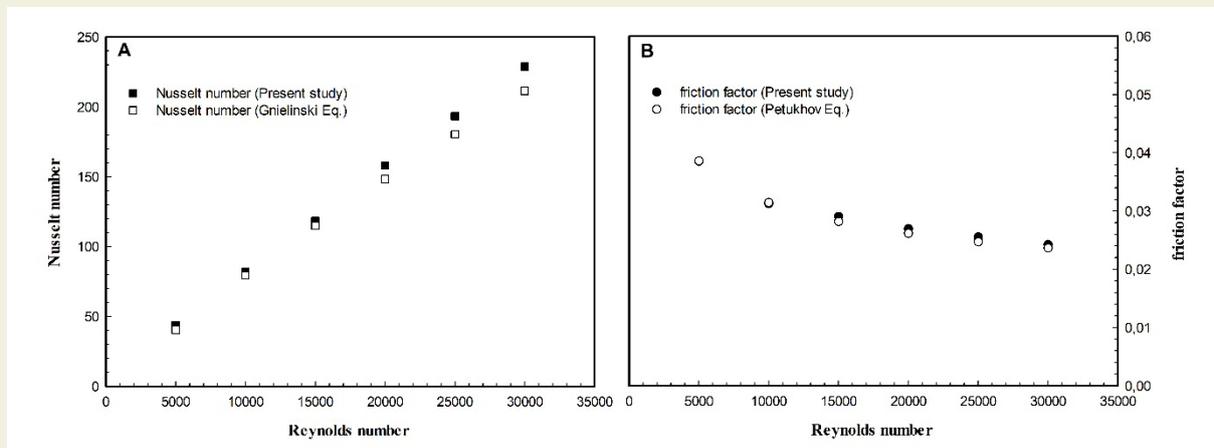


Figure 3. Validation results of numerical procedure

lion. The parameter  $y^*$ , crucial for controlling mesh models, was determined to be approximately  $y^* \approx 3$  within the boundary layer region, adhering to the condition  $y^+ < 5$  as required. Additionally, the skewness value of the mesh structure was found to be approximately  $\approx 0.6$ , while the orthogonal quality value was approximately  $\approx 0.4$ . Consequently, based on this result, the polyhedral grid structure depicted in Figure 2 was selected for further analysis.

In numerical investigations, it is essential to validate the outcomes of the analogy used for parameter evaluation by comparing them with established equations. In this study, the results obtained from the analysis using water fluid were validated with the equations provided by Gnielinski [45] and Petukhov [46] for  $Nu$  and  $f$ , respectively, as outlined in Equations 15 and 16.

$$Nu = \frac{(f/8)(Re_D - 1000)Pr}{1 + 12.7(f/8)^{1/2}(Pr^{2/3} - 1)} \quad (15)$$

$$f = (0.79 \ln(Re) - 1.64)^{-0.2} \quad (16)$$

As depicted in Figure 3, there is a remarkable agreement

between the numerical results and established equations in the assessment of the  $Nu$  (Fig.3A) and  $f$  (Fig.3B). For the smooth heat exchanger tube utilizing water fluid, the highest observed error rates fall within the range of  $\pm 5.69\%$  for the  $Nu$  and  $\pm 3.88\%$  for the  $f$ .

### 3.2. Thermal and hydraulic characteristics

As illustrated in Figure 4, the  $Nu$  exhibited an ascending trend with the rise in  $Re$  across all configurations, aligning with expectations. The volumetric ratio of the hybrid nanofluid demonstrated a positive impact on the  $Nu$ , exhibiting an increase with the addition of the nano-additive. The incorporation of circular dimple once again resulted in enhanced heat transfer, and the  $Nu$  decreased as the distance between the dimples increased.

As depicted in Figure 4, the configuration  $S5-P/D_t=1$  exhibited the most favorable thermal characteristics. The S5 fluid model comprises 0.75% GnP, 0.50% MWCNT, and 0.25%  $FE_3O_4$ , while maintaining the smallest variation in the distance between the circular dimples. In this analysis, it is substantiated that the fluid model with the highest thermal conductivity enhances thermal charac-

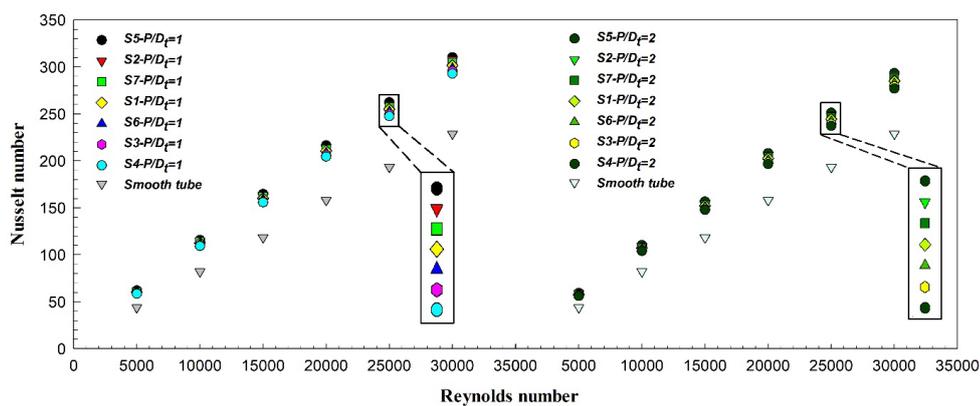


Figure 4. Distribution of  $Nu$  versus  $Re$  for all configurations

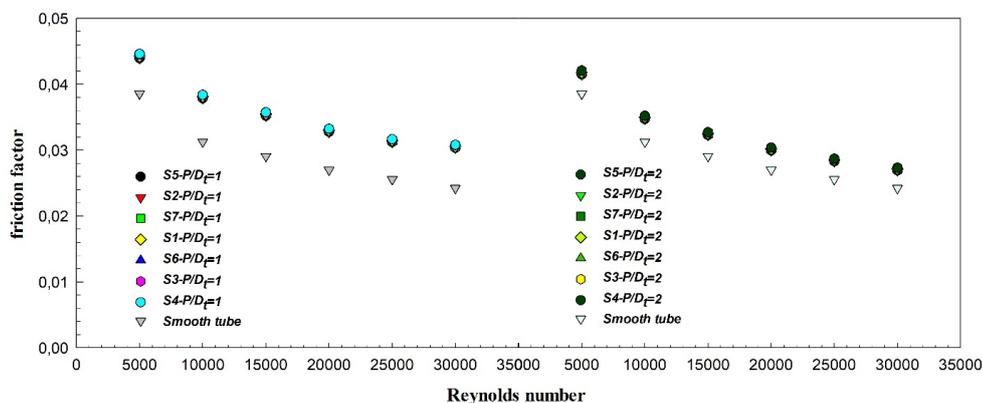


Figure 5. Distribution of  $f$  versus  $Re$  for all configurations

teristics, and the implementation of a dimple model with a short distance is conducive to promoting turbulence.

Based on the obtained results, the  $S5-P/D_t=1$  variation exhibited the highest  $Nu$ , reaching 61.87. This value is approximately 1.42 times higher than that of the smooth tube. In contrast, when the same fluid was used but with a  $P/D_t=2$  variation, the  $Nu$  was slightly lower at 59.33. The lowest  $Nu$ , which was 56, occurred at  $P/D_t=2$  for S4, representing the hybrid nanofluid model with the lowest thermal conductivity value.

As illustrated in Figure 5, the influence of hybrid nanofluid volumetric ratios on the friction coefficient appears to be quite limited. The coefficient of friction values remained approximately the same across different hybrid nanofluid mixing ratios. This consistency can be attributed to the fact that the total nanofluid volumetric ratios were consistent in all configurations.

The coefficient of friction showed an increase with the introduction of the circular dimple. Furthermore, there was a positive correlation between the coefficient of friction and the decreasing distance between the circular dimples. Conversely, a decreasing trend was observed in the coefficient of friction with an increase in  $Re$ .

Based on the results presented in Figure 5, the lowest coefficient of friction was observed for the  $S5-P/D_t=2$  configuration at a  $Re$  of 30000. In this configuration, the  $f$  increased by 1.11 times compared to the smooth tube. On the other hand, the highest  $f$ , which was 0.04458, was found for the  $S4-P/D_t=1$  model at the lowest  $Re$  of 5000.

### 3.3. Overall enhancement

In thermal systems, the implementation of heat transfer enhancement techniques is aimed at improving heat transfer, but it often comes at the cost of increased pressure drop. Recognizing that an increase in pressure drop is not a desirable outcome, Webb R.L. [47] introduced the coefficient of thermohydraulic performance. This coefficient serves as a metric to express the net energy gain in

systems where heat transfer improvement techniques are applied, offering a comprehensive assessment that considers both enhanced heat transfer and the associated increase in pressure drop.

As depicted in Figure 6, the thermohydraulic coefficient of performance for configurations employing hybrid nanofluid and circular dimple is consistently above 1. This observation suggests that the applied method is thermally and hydraulically advantageous. A coefficient of performance above 1 indicates that, despite the increase in pressure drop associated with the heat transfer enhancement techniques, the net energy gain in terms of improved heat transfer outweighs the added hydraulic losses, making the overall system more efficient.

The thermo-hydraulic results exhibit a decreasing trend with an increase in  $Re$ . Consequently, higher overall enhancement is achieved at lower  $Re$ , as the pressure drop becomes more pronounced at higher  $Re$ . Specifically, configurations with  $P/D_t=1$  demonstrate significantly better performance values, while  $P/D_t=2$  configurations, as anticipated, exhibit relatively lower performance.

The highest thermo-hydraulic coefficient of performance was achieved by the  $S5-P/D_t=1$  configuration, reaching 1.35 at the lowest  $Re$ . In contrast, for the  $P/D_t=2$  configuration within the same fluid model, this value was slightly lower at 1.32. On the other hand, the lowest performance value, amounting to 1.16, was observed at the highest  $Re$  for the  $S4-P/D_t=2$  model. These results indicate variations in performance based on different configurations and  $Re$ , with the  $S5-P/D_t=1$  configuration exhibiting the most favorable thermo-hydraulic performance under the specified conditions.

## 4. Conclusions

In conclusion, the numerical study delved into the thermal and hydraulic performance of heat exchanger configurations employing hybrid nanofluids and circular dimples. The findings offer valuable insights into various

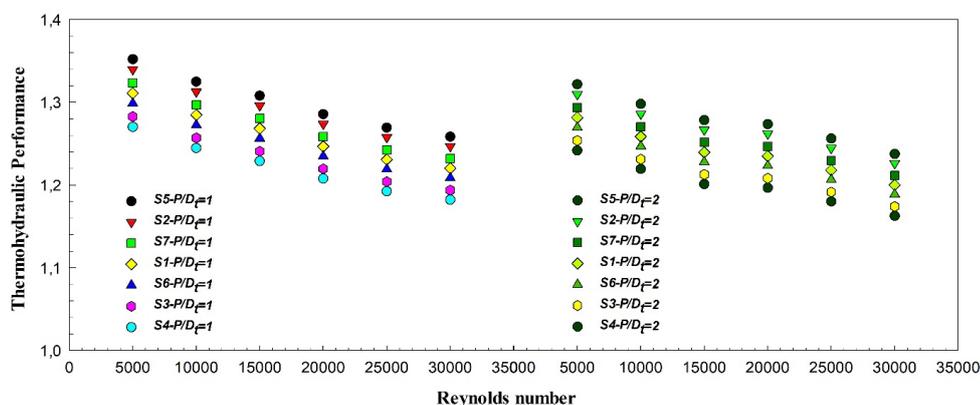


Figure 6. Distribution of thermo-hydraulic performance versus  $Re$  for all configurations

parameters, shedding light on the effectiveness of heat transfer enhancement techniques.

- The ascending trend of  $Nu$  with increasing Reynolds number was consistently evident across all configurations, with the volumetric ratio of the hybrid nanofluid demonstrating a positive correlation, and circular dimples contributing to enhanced heat transfer. Specifically, the  $S5-P/Dt=1$  configuration emerged as the most thermally favorable, showcasing superior thermal characteristics attributable to its unique fluid composition and the implementation of circular dimples with a shorter distance.
- Examining variations in the friction coefficient, the  $S5-P/Dt=2$  configuration at Reynolds number 30000 yielded the lowest coefficient, albeit 1.11 times higher than the smooth tube. Conversely, the highest friction coefficient of 0.04458 was observed for the  $S4-P/Dt=1$  model at the lowest Reynolds number of 5000.
- The thermohydraulic coefficient of performance consistently exceeded 1, indicating thermal and hydraulic advantages in configurations employing hybrid nanofluids and circular dimples. This signifies that, despite an associated increase in pressure drop, the net energy gain from improved heat transfer outweighs hydraulic losses.
- In terms of optimal performance, the  $S5-P/Dt = 1$  configuration demonstrated the highest thermohydraulic coefficient at 1.35, whereas the  $P/Dt = 2$  variation within the same fluid model exhibited a slightly lower value of 1.32. The lowest performance, amounting to 1.16, was observed at the highest Reynolds number for the  $S4-P/Dt = 2$  model.
- This comprehensive analysis offers significant insights into the intricate interplay of parameters, providing valuable guidance for the design and optimization of thermal systems employing hybrid nanofluids and circular dimples.

## Nomenclature

$c_p$	specific heat, J/kgK
$f$	friction factor

$FE_3O_4$	Iron oxide
$GnP$	Graphene nanoplatelet
$h$	convective heat transfer coefficient, W/m <sup>2</sup> K
$k$	thermal conductivity, W/mK
MWCNT	Multi-walled carbon nanotube
$Nu$	Nusselt number
$P$	pitch length, mm
$Pr$	Prandtl number
$q$	heat flux, W/m <sup>2</sup>
$Q$	rate of heat transfer, W
$r$	radius of the tube, mm
$Re$	Reynolds number
$T$	temperature, K
$V$	average velocity, m/s
$\Delta P$	pressure drop, Pa

## Greek symbols

$\rho$	density, kg/m <sup>3</sup>
$\mu$	dynamic viscosity, kg/ms
$\phi$	volume concentration, %

## Subscripts

$f$	fluid
$nf$	nanofluid
$hnf$	hybrid nanofluid
$Thnf$	ternary hybrid nanofluid
$b$	base

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