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ASSESSMENT OF WIND CHARACTERISTICS AND WIND ENERGY POTENTIAL IN WEST BLACK SEA REGION OF TURKEY

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ABSTRACT

In this study, wind characteristics and wind energy potential of seven cities from The West of Black Sea Region in Turkey were analyzed. The wind data were obtained by National State Meteorological Service. It was measured at 10 meters' height in the date range 2010-2014. Weibull probability density function was calculated and estimated Weibull shape parameter k and scale parameter c, with the data for those locations. According to the power calculations of the region, annual mean power densities of Zonguldak, Bartın, Kastamonu, Bolu, Karabük, Düzce and Sinop were calculated as 105 W/m², 37,4 W/m², 40 W/m², 27,15 W/m², 27 W/m², 26,3 W/m² and 209 W/m² at the height of 50 m, respectively. The results show that, the region has not enough wind energy potential considering investment on wind power energy except Sinop.

Keywords: Black Sea Region wind potential, Power density, Probability distribution function

1. INTRODUCTION

All over the world, the scissors between energy consumption and production is pointing that current policies are not sustainable. So, a counterpoise must be found among energy consumption, generation, security, economic development and protection of the environment. In last two decades, renewable energy sources are accepted the most convenient way and most reasonable one wind energy has been growing rapidly. Developed countries have paid more attention toward wind power energy as a clean source. Most of the European countries allocated huge budgets in last decade for wind power energy. The capacities of some EU countries are 56,132 MW in Germany, 23,074 MW in Spain, 9,479 MW in Italy, 13,759 MW in France and 18872 MW in England at the end of 2017. USA reached total capacity 89,077 MW, while Canada has got installed total capacity 12,239 MW in 2017 [1-3].

Before having a decision to setup and invest, determination wind energy potential is indispensable for a proper location [3-5]. According to theoretical calculations of economic potential of wind energy in Turkey, 70% of the energy needs of the country can be supplied approximately. Turkey's economic wind potential and technical wind potential were estimated as 48,000 MW, 88,000 MW respectively. Although the installed power of Turkey is seen on Table 1 from 2002 to 2017 [3].

As the wind is affected by the stochastic structure and local geographic conditions, it is necessary to conduct feasibility and long-term measurements before the investment in the places where wind energy investment is planned. In today's world, where energy costs and energy demand are high, wind energy potential studies are continuing all over the world. A research about Canary Islands of Spain examines the wind energy potential by various analysis methods of distribution functions [6]. The wind potential of Koronos in Greece by using the measurement results obtained from observation mast. The results were statistically analyzed by using the Weibull and Rayleigh functions. Annual mean power density was calculated as 420 W/m² [7]. For the comparison of energy capacities in Germany, the market was modeled, and wind potential effect was calculated [8].

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Table 1 Installed power capacity of Turkey by sources [2, 3].

Source Kind/Year	2002	2009	2012	2014	2015	2017	2018
	(MW)						
Thermal Energy	19569	29339	35029	41802	41903	46926	46931.9
Hydroelectrical Energy	12241	14553	19620	23643	25868	27273	28336.3
Wind Energy	19	792	2261	3630	4503	6516	6995.5
Geothermal Energy	18	77	162	405	624	1063	1239.7
Solar Energy	-	-	-	40	249	3420	5047.4
Sum	31846	44761	57071	69520	73147	85200	88550.8

Various locations wind potentials were measured and evaluated in Turkey as well. In these studies, several methods can be applied such as using measurements of Turkish State Meteorological Service (TSMS) or independent measurements or estimating statistical values by using these measurements. As the measurements of TSMS, the mean power density (222 W/m²) and average wind speed (7,3 m/s) were determined in Gaziantep Nurdagi [9]. By using the estimating methods of Weibull and Rayleigh distributions, the potential of Elazig district was calculated via the data of the results of the measurements lasting 6 years [10-11]. In some studies, the wind power potentials of various locations to find out proper zones. Regarding the results of the measurements in the southern Anatolia, Samandag was calculated most suitable location [12]. The wind potential of the North Eastern of Turkey was observed and statistically analyzed by using the measurements of six different TSMS stations. Regarding the results, the mean wind power densities are nearly same and under 59.96 W/m², which is below than weak resource range and not feasible for investment [13].

In this study, the wind potential of the West Black Sea Region was evaluated by using real wind data obtained from TSMS. The wind speed and direction as well as the availability, the duration and the diurnal variation were assessed, and the results were statistically compared with Weibull distribution functions. Distribution function with three methods, which are Least Square Method (LSM), Maximum Likelihood Method (MLM) and Moment Method (MM) were used to determine Weibull parameters.

2. WIND DATA AT WEST BLACK SEA REGION

In this study, the observation values, which were taken from the weather stations of TSMS measuring at 10 meters height in Zonguldak, Bartın, Kastamonu, Bolu, Karabük, Düzce and Sinop provinces in the western black sea region, were used. The measurement data consist of hourly wind data between the years 2010-2014. Wind speed, direction, pressure, humidity and temperature values were obtained from the measurement stations which were given satellite images in Fig. 1. Descriptive statistical wind speed values of the measurement stations are seen on Table 2. Obtained wind speed values in the measurement results were extrapolated to 50 m via Eq.5. for energy potential calculation and the descriptive statistics of these transformed values are given on Table 3.

The wind speed data were analyzed at the measurement height. The central tendencies were calculated. Descriptive statistics were given on Table 2..The central tendency was defined as seen on Eq.(1), where \bar{v} is the mean value, v_i is the data sequence and n is the number of the data contained in this data sequence. The discrete degree of the data sequence relative to the mean value was obtained by the Standard deviation (Std) value as seen on Eq. (2). The distributional pattern of the data was obtained by using Skewness and Kurtosis as seen on Eq. (3) and Eq. (4) respectively [14]:



Figure 1 The locations of the weather stations

$$\bar{V} = \frac{1}{n} \sum_{i=1}^{n} V_i$$

$$\sigma = Std = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (V_i - \bar{V})^2}$$

$$\tag{2}$$

$$\sigma = Std = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (V_i - \overline{V})^2}$$
 (2)

Skewness =
$$\frac{1}{n-1} \sum_{i=1}^{n} \frac{(V_i - \bar{V})^3}{\sigma^3}$$
 (3)

$$Kurtosis = \frac{1}{n-1} \sum_{i=1}^{n} \frac{(V_i - \bar{V})^4}{\sigma^4} - 3$$
 (4)

Table 2. Description Statistics (10 m Observed)

	Zonguldak	Bartın	Kastamonu	Bolu	Karabük	Düzce	Sinop
Mean	2,1900	2,1900	1,5109	1,3984	1,1475	1,1475	2,8627
Std	1,4830	1,4830	0,9122	0,9505	0,8472	0,8463	2,0083
Skewness	13,2161	13,2161	5,0283	4,0883	9,2564	5,0318	7,0559
Kurtosis	2,4220	2,4220	1,6923	1,6730	2,5252	1,9390	1,8335
Max	23,600	23,600	11,900	11,500	11,000	9,100	27,900

Table 3. Description Statistics (50 m Calculated)

	Zonguldak	Bartın	Kastamonu	Bolu	Karabük	Düzce	Sinop
Mean	2,7298	2,7298	1,8832	1,7431	1,4304	1,4376	3,5862
Std	1,8633	1,8633	1,1477	1,1942	1,0635	1,0602	2,5159
Skewness	13,041	13,041	4,9426	4,0437	9,1793	5,0318	7,0559
Kurtosis	2,3949	2,3949	1,6643	1,6566	2,5051	1,9390	1,8335
Max	29,5643	29,5643	14,9074	14,4063	13,7800	11,3998	34,951



Figure 2. The wind roses of the locations are listed as: (a) Zonguldak; (b) Bartın; (c) Kastamonu; (d) Bolu; (e) Karabük; (f) Bartın; (g) Sinop

Table 4. Description Statistics (50 m Calculated)

	Zonguldak	Bartın	Kastamonu	Bolu	Karabük	Düzce	Sinop
Mean	2,7298	2,7298	1,8832	1,7431	1,4304	1,4376	3,5862
Std	1,8633	1,8633	1,1477	1,1942	1,0635	1,0602	2,5159
Skewness	13,041	13,041	4,9426	4,0437	9,1793	5,0318	7,0559
Kurtosis	2,3949	2,3949	1,6643	1,6566	2,5051	1,9390	1,8335
Max	29,5643	29,5643	14,9074	14,4063	13,7800	11,3998	34,951

Table 5. The wind speed densities of the weather stations

vr	Zonguldak	Bartın	Kastamonu	Bolu	Karabük	Düzce	Sinop
0-0,5	0,0168	0,1691	0,0467	0,0645	0,0880	0,1130	0,0167
0,5-1,5	0,3415	0,5503	0,5426	0,5943	0,6995	0,6419	0,2468
1,5-2,5	0,3307	0,1539	0,2816	0,2082	0,1407	0,1437	0,2386
2.5-3.5	0,1570	0,0742	0,0857	0,0882	0,0402	0,0543	0,1811
3.5-4.5	0,0809	0,0337	0,0300	0,0330	0,0199	0,0214	0,1273
4.5-5.5	0,0374	0,0122	0,0096	0,0090	0,0084	0,0050	0,0792
5.5-6.5	0,0181	0,0043	0,0026	0,0019	0,0026	0,0013	0,0451
6.5-7.5	0,0084	0,0014	0,0009	0,0005	0,0003	0,0002	0,0225
7.5-8.5	0,0039	0,0006	0,0002	0,0003	0,0003	0,0000	0,0114
8.5-9.5	0,0021	0,0002	0,0000	0,0001	0,0001	0,0000	0,0062
9.5-10.5	0,0012	0,0000	0,0000	0,0001	0,0000	0,0000	0,0043
10.5-11.5	0,0007	0,0001	0,0000	0,0000	0,0000	0,0000	0,0026
11.5-12.5	0,0004	0,0000	0,0000	0,0000	0,0000	0,0000	0,0015
12.5-13.5	0,0002	0,0000	0,0000	0,0000	0,0000	0,0000	0,0012
13.5-14.5	0,0001	0,0000	0,0000	0,0000	0,0000	0,0000	0,0006
14.5-15.5	0,0001	0,0000	0,0000	0,0000	0,0000	0,0000	0,0003
15.5-16.5	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0002
16.5-17.5	0,0001	0,0000	0,0000	0,0000	0,0000	0,0000	0,0001
17.5-18.5	0,0001	0,0000	0,0000	0,0000	0,0000	0,0000	0,0001
18.5-19.5	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0002
19.5-20.5	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000

3. WIND CHARECTERISTIC AND PROBABILTY MODELS

3.1. Variation of Wind Speed with Height

Generally, the wind speed measurements have been made at 10 m height. The wind data used in this study is extrapolated 50 m height above ground level. It is known that the wind speed is proportional to height. Extrapolation of the wind speed was made by Eq. (5), where V_o and V are the wind speeds at the standard height 10 m and at the hub height h m, respectively, and a is the roughness factor. The theoretical variation of the wind speed depending on the height varies between 0.08 and 0.4. In this study, we took the measurement sites as 0.14 by accepting open ridges and open land cover [5].

$$\frac{V}{V_o} = \left(\frac{h}{h_0}\right)^{\alpha} \tag{5}$$

By substituting h=50 and the measured wind speed data at the standard height 10 m to Eq. (5), wind speed values at the hub height are obtained.

3.2. Probability Models

Weibull probability distribution function (pdf) is as follows [15];

$$f(V) = \frac{k}{c} \left(\frac{V}{c}\right)^{k-1} exp\left(-\left(\frac{V}{c}\right)^{k}\right), (k > 0, c > 0, V > 0)$$
(6)

The cumulative distribution function (cdf) of two parameter weibull distribution is as follows [15]

$$F(V) = 1 - exp\left[-\left(\frac{V}{c}\right)^{k}\right] \tag{7}$$

In this formula (7); k represents shape parameter, c represents the scale parameter (m/s) and V is observed wind speed data [6,14].

3.1.1. Least square method (LSM)

Weibull distribution parameter is found with least square method by Eq. (8) and Eq. (9), [15,16],

$$y_{i} = \left[\ln\left(-\ln\left(1 - F(v_{i})\right)\right)\right]$$

$$k = \frac{n\sum_{i=1}^{n}(\ln v_{i}) y_{i} - \sum_{i=1}^{n}\ln v_{i}\sum_{i=1}^{n}y_{i}}{n\sum_{i=1}^{n}\ln(v_{i}^{2}) - \left[\sum_{i=1}^{n}\ln v_{i}\right]^{2}}$$

$$k = \frac{n \sum_{i=1}^{n} \ln(v_i^2) - [\sum_{i=1}^{n} \ln v_i]^2}{n \sum_{i=1}^{n} \ln(v_i^2) - [\sum_{i=1}^{n} \ln v_i]^2}$$
(8)

$$c = exp\left[\frac{k\sum_{i=1}^{n} \ln v_i - \sum_{i=1}^{n} \ln(-\ln(1 - F(v_i)))}{n.k}\right]$$
(9)

3.1.2. Maximum likelihood method (MLM)

With maximum likelihood method, standard iterative techniques or Newton Raphson method or trialerror techniques can be used. After numerical solution of the found as follows [6].

$$\frac{\sum_{i=1}^{n} v_i^k \ln v_i}{\sum_{i=1}^{n} v_i^k} - \frac{\sum_{i=1}^{n} \ln v_i}{n} - \frac{1}{k} = 0$$
 (10)

$$c = \left(\frac{\sum_{i=1}^{n} v_i^k}{n}\right)^{\frac{1}{k}} \tag{11}$$

3.1.3. Moment method (MM)

In this paper, also with Moment method, k and c parameters are obtained using Eq. (11) and Eq. (12) respectively, using average wind speed (\bar{v}) and standard deviation (σ) of observed wind speed [3].

$$k = \left(\frac{\sigma}{\bar{v}}\right)^{-1,086} \tag{12}$$

The c scale parameter was calculated by Eq. (12) using the mean velocity (\bar{v}) , the gamma function Γ () and the k computed in Eq. (11).

$$c = \frac{\bar{v}}{\Gamma\left(1 + \frac{1}{k}\right)} \tag{13}$$

The wind speed distributions measured for each province are given in Figure 3 with the wind speed density graphs obtained by Weibull probability distribution function for different parameter estimation methods with histograms graphs and the calculated distribution parameters are given in Table 7..

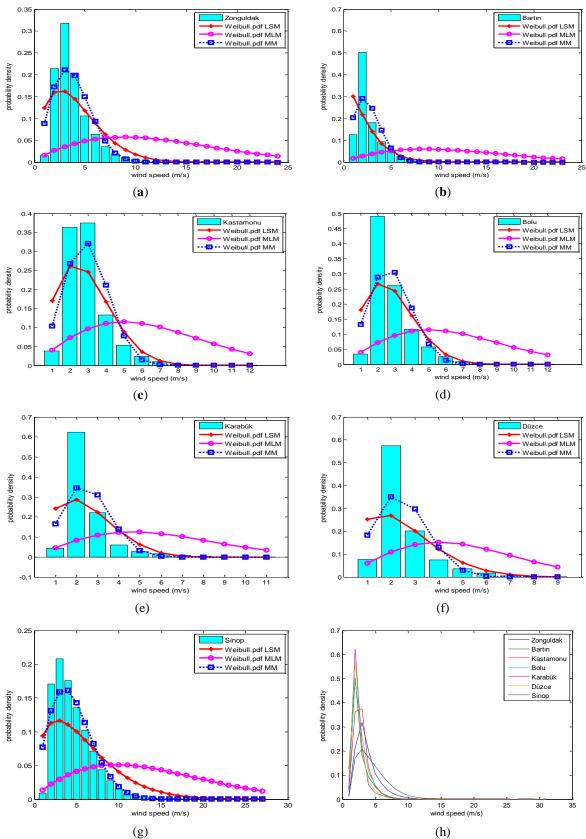


Figure 3. The wind speed densities observed and obtained from Weibulls are listed as: (a) Zonguldak; (b) Bartın; (c) Kastamonu; (d) Bolu; (e) Karabuk; (f) Bartın; (g) Sinop (h) All stations wind speed density observed.

	Parameters	LSM	MLM	MM
Zonguldak	k	1,6461	1,7995	2,1787
	c	4,6389	1,3419	4,2694
Bartın	k	1,2051	1,7995	2,0107
	c	2,3503	13,4190	2,9513
Kastamonu	k	2,0286	1,9314	2,6969
	c	3,2415	7,3100	3,3044
Bolu	k	1,9937	1,9314	2,5089
	c	3,1689	7,3100	3,1667
Karabük	k	1,8225	1,9554	2,5512
	c	2,7847	6,7529	2,8407
Düzce	k	1,6594	2,0187	2,4701
	c	2,7863	5,6372	2,7777
Sinop	k	1,4379	1,7768	1,9432
	c	6,3370	15,6358	5,1611

Table 6 Estimating Weibull parameters for weather stations

4. EVALUATION CRITERIA

Root Mean Square Summations of Error test (RMSE) and R squared (R^2) were used to evaluate the performance of the Weibull distribution and parameter estimating methods. The RMSE parameter gives the deviation between the predicted and the measurement values. The RMSE value must be as converge to zero as possible, and its equation follow as:

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (V_{ci} - V_{oi})^{2}}$$
T
(14)

Table 7. Performance of Weibull models with actual wind speed density

Model Performance	Criteria	LSM	MLM	MM
Zonguldak	RMSE	0.0437	0.0852	0.0306
	R^2	0.9549	0.959	0.9561
Bartın	RMSE	0.0702	0.1125	0.0503
	R^2	0.8539	0.9274	0.8663
Kastamonu	RMSE	0.0626	0.1291	0.0439
	R^2	0.8722	0.8652	0.8895
Bolu	RMSE	0.0788	0.1411	0.0691
	R^2	0.8412	0.8558	0.8322
Karabük	RMSE	0.1214	0.1789	0.0980
	R^2	0.7171	0.7840	0.7077
Düzce	RMSE	0.1188	0.1705	0.0900
	R^2	0.7695	0.7738	0.7592
Sinop	RMSE	0.0319	0.0625	0.0185
-	R^2	0.9831	0.9794	0.9840

Modelling Efficiency (EF) or called R^2 represents the ability of the model. Determination Coefficient (R^2) value is aimed to be as close as 1.0 to fit the regression line and the data well. R^2 can be calculated via Eq. (15) [19]:

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (V_{ci} - V_{i})^{2}}{\sum_{i=1}^{n} (V_{ci} - \overline{V_{o}})^{2}}$$
 (15)

Vi is the ith experimental data, \overline{Vo} is the mean value of the experimental data, Vci is the ith predicted 234

data with the Weibull distribution and n is the number of measurements.

For each province, Table 7 shows the measured wind speed distribution frequencies and the wind speed density values obtained by the Weibull probability distribution function for different parameter estimation methods according to the performance criteria (RMSE and R^2).

5. ASSESSMENT OF WIND POWER POTENTIAL

The power in the wind passing through an area A perpendicular to the wind is given by

$$P_{W} = \frac{1}{2}\rho A V^{3} \ (W) \tag{16}$$

The average wind power is then

$$\overline{P_W} = \frac{1}{2} \rho A \sum_{i=1}^{n} p(V_i) V_i^3 \quad (W)$$
 (17)

The probabilities $p(V_i)$ are determined from the actual wind data. If it is modelled the actual wind data by a probability density function $f(V_i)$, the average power is in wind is as follows [18].

$$P_{W} = \frac{1}{2}\rho A \int_{0}^{\infty} V^{3} f(V) dV \quad (W)$$
 (18)

The average power can be shown Eq. (19), where; ρ air density, A is an area wind passing through, k is shape parameter of the Weibull distribution function f(V) and $\Gamma(V)$ is gamma function [17-19].

$$P_{w} = \frac{1}{2} \frac{\rho A V^{3} \Gamma(1 + \frac{3}{k})}{\left[\Gamma(1 + \frac{1}{k})\right]^{3}} \quad (W)$$
 (19)

So, for per unit area wind power density can be express,

$$\frac{\overline{P_w}}{A} = \frac{1}{2} \rho \int_0^\infty V^3 f(V) dV \quad (W/m^2)$$
 (20)

For each province, the calculated actual mean wind power density and the Weibull probability distribution function power density results for different parameter estimation methods are given in Table 8.

Table 8 Actual power density and obtain with Weibull and for weather stations

Power Density (W/m²)	Actual	LSM	MLM	MM
Zonguldak	105,1000	170,6000	2177,7000	95,2000
Bartın	37,4000	42,7000	2177,7000	34,0000
Kastamonu	40,0038	44,6150	347,6355	37,9872
Bolu	37,1514	42,4440	34,7636	34,9069
Karabük	27,2100	29,3800	27352,0000	24,9300
Düzce	26,3025	46,8968	273,5172	23,9165
Sinop	209,7000	545,0000	3453,3000	188,6000

6. CONCLUSION

In this study, yearly wind speed distribution and wind power density during the period of 2010–2014 in the seven stations of West Black Sea Region in Turkey were evaluated. It can be concluded as follows.

- The maximum value of hourly mean wind speed is determined as 2.86 m/s at Sinop in five years period and a minimum value of 1,14 m/s is occurred at Karabük in the same period. A maximum value of hourly mean wind speed is obtained at Sinop as 27,9 m/s.
- The mean annual value of Weibull shape parameter k is between 1.2051 and 2.5512 while the annual value of scale parameter c is between 1,3419 and 15,6318 m/s.
- The most windward directions at Bartin and Düzce are north and southwest, while the direction at Zonguldak and Sinop are southeast, Kastamonu are SSW and NNE, Bolu is SW and Karabük is WNW.
- The yearly mean wind power densities for Zonguldak, Bartın, Kastamonu, Bolu, Karabük, Düzce and Sinop are calculated to be 105 W/m², 37,4 W/m², 40 W/m², 37,15 W/m², 27 W/m² 26,3 W/m² and 209 W/m² at the height of 50 m, respectively.
- The current study is an investigation study in order to estimate wind energy potential of the seven locations of the West Black Sea Region in Turkey. These locations investigated in this study can be evaluated.

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